References for Research in Quantum Distinguishability and State Disturbance

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(22 September 1996)

Abstract

This document contains 578 references that may be useful in answering the following questions in all their varied contexts: "How statistically distinguishable are quantum states?" and "What is the best tradeoff between disturbance and inference in quantum measurement?"

References are grouped under three major headings: Progress Toward the Quantum Problem; Information Theory and Classical Distinguishability; and Matrix Inequalities, Operator Relations, and Mathematical Techniques.

This is an expanded version of the bibliography appearing in my Ph. D. Dissertation *Distinguishability* and *Accessible Information in Quantum Theory*. Even now, the list is far from complete: relevant additions to the list are welcome. Eventually, this bibliography will be annotated and published elsewhere.

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